

Problem 1. Let f be a function given by

$$f(x) = x^3 - 10x + 9.$$

(a) Find the zeros of f . (Hint: first note that $f(1) = 0$.)

(b) Write an equation of the line tangent to the graph of f at $x = -1$.

(c) Find the number $c \in (a, b)$ such that

$$f'(c) = \frac{f(b) - f(a)}{b - a}$$

on the closed interval $[a, b] = [1, 3]$.

Problem 2. Let

$$f(x) = x^4 - 13x^2 + 36.$$

(a) Find all zeros of f , zeros of f' , and zeros of f'' .

(b) Find the maximal intervals on which f is positive, negative, increasing, decreasing, concave up, or concave down.